

Many accents have been re-defined

`c \c{c} \pi \cpi`

$c\pi\pi$

`int \e{\im x} \d{x}`

$$\int e^{ix} dx$$

`\^{\beta_1}=b_1`

$$\widehat{\beta}_1 = b_1$$

`\=x=\frac{1}{n}\sum x_i`

$$\bar{x} = \frac{1}{n} \sum x_i$$

`\b{x} = \frac{1}{n} \wrap[()]{x_1 + \dots + x_n}`

$$\bar{x} = \frac{1}{n} (x_1 + \dots + x_n)$$

Sometimes overline is better: `\b{x}` vs. `\ol{x}`

$\bar{x}$  vs.  $\overline{x}$

And, underlines are nice too: `\ul{x}`

$\underline{x}$

A few other nice-to-haves:

`\Gamma[n+1]=n!`

$$\Gamma(n+1) = n!$$

`\binom{n}{x}`

$$\binom{n}{x}$$

`\e{x}`

$e^x$

`\logit \wrap{p} = \log \wrap{\frac{p}{1-p}}`

$$\text{logit } [p] = \log \left[ \frac{p}{1-p} \right]$$

Common distributions along with other features follows:

Normal Distribution

$Z \sim N(0, 1)$ , where  $E[Z] = 0$  and  $V[Z] = 1$

$$Z \sim N(0, 1), \text{ where } E[Z] = 0 \text{ and } V[Z] = 1$$

$P\{|Z| > z_{\alpha}\} = \alpha$

$$P\left[|Z| > z_{\frac{\alpha}{2}}\right] = \alpha$$

$p_N(z)$

$$\frac{1}{\sqrt{2\pi}} e^{-z^2/2}$$

or, in general

$p_N(z; \mu, \sigma^2)$

$$\frac{1}{\sqrt{2\pi\sigma^2}} e^{-(z-\mu)^2/2\sigma^2}$$

Sometimes, we subscript the following operations:

$E_z[Z] = 0$ ,  $V_z[Z] = 1$ , and  $P_z\{|Z| > z_{\alpha}\} = \alpha$

$$E_z[Z] = 0, V_z[Z] = 1, \text{ and } P_z\left[|Z| > z_{\frac{\alpha}{2}}\right] = \alpha$$

Multivariate Normal Distribution

$\mathbf{X} \sim N_p(\boldsymbol{\mu}, \boldsymbol{\Sigma})$

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Chi-square Distribution

$Z_i \stackrel{iid}{\sim} N(0, 1)$ , where  $i = 1, \dots, n$

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$\chi^2 = \sum_i Z_i^2 \sim \chi^2(n)$

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$p_{\chi^2}(z)$

$$\frac{2^{-n/2}}{\Gamma(n/2)} z^{n/2-1} e^{-z/2} I_z(0, \infty), \text{ where } n > 0$$

t Distribution

$\frac{N(0, 1)}{\sqrt{\frac{\chi^2(n)}{n}}} \sim t(n)$

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F Distribution

$X_i, Y_{\tilde{i}} \stackrel{\text{iid}}{\sim} N(0, 1)$  where  $i = 1, \dots, n; \tilde{i} = 1, \dots, m$  and  $V[X_i, Y_{\tilde{i}}] = \sigma_{xy} = 0$

$\chi_x^2 = \sum_i X_i^2 \sim \chi^2(n)$

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$\chi_y^2 = \sum_{\tilde{i}} Y_{\tilde{i}}^2 \sim \chi^2(m)$

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$\frac{\chi_x^2}{\chi_y^2} \sim F(n, m)$

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Beta Distribution

$B = \frac{\frac{n}{m}F}{1 + \frac{n}{m}F} \sim \text{Beta}\left(\frac{n}{2}, \frac{m}{2}\right)$

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$p_{\text{Beta}}(\alpha, \beta)$

$$\frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1} \mathbf{I}_x(0, 1), \text{ where } \alpha > 0 \text{ and } \beta > 0$$

Gamma Distribution

$G \sim \text{Gam}(\alpha, \beta)$

$$G \sim \text{Gamma}(\alpha, \beta)$$

$p_{\text{Gam}}(\alpha, \beta)$

$$\frac{\beta^\alpha}{\Gamma(\alpha)} x^{\alpha-1} e^{-\beta x} \mathbf{I}_x(0, \infty), \text{ where } \alpha > 0 \text{ and } \beta > 0$$

Cauchy Distribution

$C \sim \text{Cau}(\theta, \nu)$

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$p_{\text{Cau}}(\theta, \nu)$

$$\frac{1}{\nu\pi \left\{1 + \left[\frac{(x - \theta)}{\nu}\right]^2\right\}}, \text{ where } \nu > 0$$

Uniform Distribution

$X \sim \mathcal{U}\{0, 1\}$

$$X \sim U(0, 1)$$

$\mathcal{p}\mathcal{U}\{0\}\{1\}$

$$I_x(0, 1)$$

or, in general

$\mathcal{p}\mathcal{U}\{a\}\{b\}$

$$\frac{1}{b-a} I_x(a, b), \text{ where } a < b$$

Exponential Distribution

$X \sim \mathcal{Exp}\{\lambda\}$

$$X \sim \text{Exp}(\lambda)$$

$\mathcal{p}\mathcal{Exp}\{\lambda\}$

$$\frac{1}{\lambda} e^{-x/\lambda} I_x(0, \infty), \text{ where } \lambda > 0$$

Hotelling's  $T^2$  Distribution

$X \sim \mathcal{Tsq}\{\nu_1, \nu_2\}$

$$X \sim T^2(\nu_1, \nu_2)$$

Inverse Chi-square Distribution

$X \sim \mathcal{IC}\{\nu\}$

$$X \sim \chi^{-2}(\nu)$$

Inverse Gamma Distribution

$X \sim \mathcal{IG}\{\alpha, \beta\}$

$$X \sim \text{Gamma}^{-1}(\alpha, \beta)$$

Pareto Distribution

$X \sim \mathcal{Par}\{\alpha, \beta\}$

$$X \sim \text{Pareto}(\alpha, \beta)$$

$\mathcal{p}\mathcal{Par}\{\alpha\}\{\beta\}$

$$\frac{\beta}{\alpha(1+x/\alpha)^{\beta+1}} I_x(0, \infty), \text{ where } \alpha > 0 \text{ and } \beta > 0$$

Wishart Distribution

$\mathcal{sfs1}\{X\} \sim \mathcal{W}\{\nu, \mathcal{sfs1}\{S\}\}$

$$X \sim \text{Wishart}(\nu, S)$$

Inverse Wishart Distribution

$\backslash\text{sfs1}\{X\} \sim \backslash\text{IW}\{\nu, \backslash\text{sfs1}\{S^{-1}\}\}$

$$X \sim \text{Wishart}^{-1}(\nu, S^{-1})$$

Binomial Distribution

$X \sim \backslash\text{Bin}\{n, p\}$

$$X \sim \text{Bin}(n, p)$$

$\backslash\text{pBin}\{n\}\{p\}$

$$\binom{n}{x} p^x (1-p)^{n-x} \mathbb{I}_x(\{0, 1, \dots, n\}), \text{ where } p \in (0, 1) \text{ and } n = 1, 2, \dots$$

Bernoulli Distribution

$X \sim \backslash\text{B}\{p\}$

$$X \sim \text{B}(p)$$

Beta-Binomial Distribution

$X \sim \backslash\text{BB}\{p\}$

$$X \sim \text{Beta-Bin}(p)$$

$\backslash\text{pBB}\{n\}\{\alpha\}\{\beta\}$

$$\frac{\Gamma(n+1)\Gamma(\alpha+x)\Gamma(n+\beta-x)\Gamma(\alpha+\beta)}{\Gamma(x+1)\Gamma(n-x+1)\Gamma(n+\alpha+\beta)\Gamma(\alpha)\Gamma(\beta)} \mathbb{I}_x(\{0, 1, \dots, n\}), \text{ where } \alpha > 0, \beta > 0 \text{ and } n = 1, 2, \dots$$

Negative-Binomial Distribution

$X \sim \backslash\text{NB}\{n, p\}$

$$X \sim \text{Neg-Bin}(n, p)$$

Hypergeometric Distribution

$X \sim \backslash\text{HG}\{n, M, N\}$

$$X \sim \text{Hypergeometric}(n, M, N)$$

Poisson Distribution

$X \sim \backslash\text{Poi}\{\mu\}$

$$X \sim \text{Poisson}(\mu)$$

$\backslash\text{pPoi}\{\mu\}$

$$\frac{1}{x!} \mu^x e^{-\mu} \mathbb{I}_x(\{0, 1, \dots\}), \text{ where } \mu > 0$$

Dirichlet Distribution

$\backslash\text{bm}\{X\} \sim \backslash\text{Dir}\{\alpha_1 \backslash. \alpha_k\}$

$$\mathbf{X} \sim \text{Dirichlet}(\alpha_1 \dots \alpha_k)$$

Multinomial Distribution

$\backslash\text{bm}\{X\} \sim \backslash\text{M}\{n, \alpha_1 \backslash. \alpha_k\}$

$$\mathbf{X} \sim \text{Multinomial}(n, \alpha_1 \dots \alpha_k)$$

To compute critical values for the Normal distribution, create the NCRIT program for your TI-83 (or equivalent) calculator. At each step, the calculator display is shown, followed by what you should do (■ is the cursor):

```

■
PRGM →NEW→1:Create New
Name=■
NCRIT ENTER
:■
PRGM →I/O→2:Prompt
:Prompt ■
ALPHA A, ALPHA T ENTER
:■
2nd DISTR →DISTR→3:invNorm(
:invNorm(■
1-(ALPHA A ÷ ALPHA T)) STO⇒ ALPHA C ENTER
:■
PRGM →I/O→3:Disp
:Disp ■
ALPHA C ENTER
:■
2nd QUIT

```

Suppose A is  $\alpha$  and T is the number of tails. To run the program:

```

■
PRGM →EXEC→NCRIT
prgmNCRIT■
ENTER
A=?■
0.05 ENTER
T=?■
2 ENTER
1.959963986

```